

Investigate the stability of zero solution using the Lyapunov's theorem:

$$1. \quad \begin{cases} \dot{x} = 2xy - x + y \\ \dot{y} = 5x^4 + y^3 + 2x - 3y \end{cases}$$

$$2. \quad \begin{cases} \dot{x} = x^2 + y^2 - 2x \\ \dot{y} = 3x^2 - x + 3y \end{cases}$$

$$3. \quad \begin{cases} \dot{x} = e^{x+2y} - \cos(3x) \\ \dot{y} = \sqrt{4+8x} - 2e^y \end{cases}$$

$$4. \quad \begin{cases} \dot{x} = \ln(4y + e^{-3x}) \\ \dot{y} = 2y - 1 + \sqrt[3]{1-6x} \end{cases}$$

$$5. \quad \begin{cases} \dot{x} = \ln(3e^y - 2 \cos x) \\ \dot{y} = 2e^x - \sqrt[3]{8+12y} \end{cases}$$

$$6. \quad \begin{cases} \dot{x} = \operatorname{tg}(y-x) \\ \dot{y} = 2^y - 2 \cos\left(\frac{\pi}{3} - x\right) \end{cases}$$

$$7. \quad \begin{cases} \dot{x} = \operatorname{tg}(z-y) - 2x \\ \dot{y} = \sqrt{9+12x} - 3e^y \\ \dot{z} = -3y \end{cases}$$

$$8. \quad \begin{cases} \dot{x} = e^x - e^{-3z} \\ \dot{y} = 4z - 3 \sin(x+y) \\ \dot{z} = \ln(1+z-3z) \end{cases}$$

Investigate, at which values of parameters (a, b) the zero solution is stable:

$$9. \quad \begin{cases} \dot{x} = ax - 2y + x^2 \\ \dot{y} = x + y + xy \end{cases}$$

$$10. \quad \begin{cases} \dot{x} = ax + y + x^2 \\ \dot{y} = x + ay + y^2 \end{cases}$$

$$11. \quad \begin{cases} \dot{x} = x + ay + y^2 \\ \dot{y} = bx - 3y - x^2 \end{cases}$$

$$12. \quad \begin{cases} \dot{x} = y + \sin x \\ \dot{y} = ax + by \end{cases}$$

$$13. \quad \begin{cases} \dot{x} = 2e^{-x} - \sqrt{4+ay} \\ \dot{y} = \ln(1+x+ay) \end{cases}$$

$$14. \quad \begin{cases} \dot{x} = \ln(e+ax) - e^y \\ \dot{y} = bx + \operatorname{tgy} \end{cases}$$

Investigate the stability of the solution:

$$15. \quad \begin{aligned} &x_0 = -t^2, \quad y_0 = t \\ &\begin{cases} \dot{x} = y^2 - 2ty - 2y - x \\ \dot{y} = 2x + 2t^2 + e^{2t-2y} \end{cases} \end{aligned}$$

$$16. \quad \begin{aligned} &x_0 = \cos t, \quad y_0 = 2 \sin t \\ &\begin{cases} \dot{x} = \ln\left(2 + 2 \sin^2 \frac{t}{2}\right) - \frac{y}{2} \\ \dot{y} = (4-x^2) \cos t - 2x \sin^2 t - \cos^3 t \end{cases} \end{aligned}$$

Investigate the stability of the zero solution using the Hurwitz condition

17. $y''' + y'' + y' + 2y = 0$

18. $y''' + 2y'' + 2y' + 3y = 0$

19. $y^{(4)} + 2y'' + 4y'' + 3y' + 2y = 0$

20. $y^{(4)} + 2y'' + 3y'' + 7y' + 2y = 0$

21. $y^{(4)} + 13y'' + 16y'' + 55y' + 76y = 0$

22. $y^{(4)} + 8y'' + 14y'' + 36y' + 45y = 0$

23. $y^{(5)} + 2y^{(4)} + 5y'' + 6y'' + 5y' + 2y = 0$

24. $y^{(5)} + 4y^{(4)} + 9y'' + 16y'' + 19y' + 13y = 0$

25. $y^{(5)} + 4y^{(4)} + 16y'' + 25y'' + 13y' + 9y = 0$

26. $y^{(5)} + 5y^{(4)} + 15y'' + 48y'' + 44y' + 74y = 0$

27. $y^{(5)} + 2y^{(4)} + 14y'' + 36y'' + 23y' + 68y = 0$